

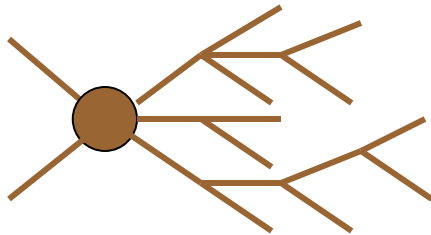
# Using Object Correlations to Extract New Physics from the LHC

Shan-Huei Chuang, Rouven Essig, Michael Graesser,  
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Sunil Somalwar, Scott Thomas

Rutgers HEX + HET

# New Physics at the Large Hadron Collider

- Extract Signatures from Data
- Interpret Signatures
- Determine Underlying Theoretical Framework

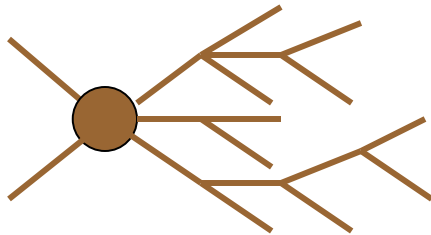


Hard Scattering Processes -  
Produce Low Multiplicity States -  
Decay to “Stable” SM Particles

Relatively Long Lived Intermediate States:  $\Gamma/m \ll 1$

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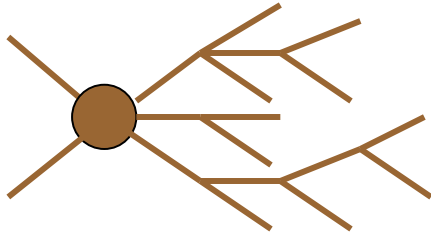
Relatively Long Lived Intermediate States:  $\Gamma/m \ll 1$

- Most Direct Route to Interpretation - Direct Measurements

Masses

Quantum Numbers (Gauge, Global, Spin, ...)

Interactions



S-Matrix =  $f(m_{ijk\dots}^2)$  (Unpolarized,

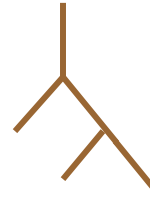
Spins

$m_{ijk\dots}^2 = f(m_{ij}^2)$

T-Invariance )

- Correlations in Generalized Dalitz Space  $m_{ij}^2$   $i,j =$  All Final State Pairs

True of Subprocess Also



Depend Directly on Masses, Quantum Numbers, Interactions

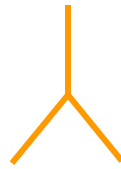
- Exploit (Subprocess) Correlations to Make Direct Measurements ...

Compare: Indirect Interpretation of Signatures

Cuts + Number Counts

# Correlations Within Decay Trees $\Gamma/m \ll 1$

3-Point Interaction



$$f(p_1^2, p_2^2, p_3^2)$$

On Shell Amplitude (Almost) Uniquely Determined by Lorentz Invariance up to Momentum Dependent Form Factor

$$J = \frac{1}{2}, \frac{1}{2}, 0$$

$$\psi_i \psi_j \phi + \text{h.c.}$$

$$J = \frac{1}{2}, \frac{1}{2}, 1$$

$$\psi_i^* \sigma^\mu \psi_j A_\mu$$

$$\psi_i \sigma^{\mu\nu} \psi_j F_{\mu\nu} + \text{h.c.}$$

.....

Near Mass Shell

$$f(p_i^2) = f_0 + (p_i^2 - m_i^2) \frac{\partial f(p_i^2)}{\partial (p_i^2 - m_i^2)} + \dots \quad i = 1, 2, 3$$

Form Factor Nearly Constant  $\Gamma/m \ll 1$

# Consistent OnShell Effective Theory (COSET)

OnShell fields  $\Psi_0, \phi_0, \dots$        $\langle \Psi_0(p) \Psi_0(-p) \rangle = -2\pi i \delta(p^2 - m^2) + \dots$

Interactions  $\Psi_0 \Psi_0 \phi_0 + \dots$

Expansion Parameters  $\Gamma/m, m/M$

OffShell fields  $\Psi, \phi, \dots$



(Radiation)

Effective Theory – Distinct from - Wilsonian Effective Theory  
Momentum Expansion  $p^2/M^2, p^2=0$   
- Heavy Field Expansion

Two Body Decay Interactions Determined to Leading Order  
- Completely in Terms of One or Two Parameters

Resummation of Wilsonian Effective Theory – Very Close Measured Experimentally

4-Point Interaction



$$f(p_1^2, p_2^2, p_3^2, p_4^2, p_{23}^2, p_{34}^2)$$

Amplitude Not Uniquely Determined -  
Form Factor Depends on Two Invariants even On Shell

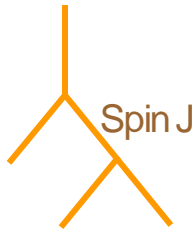
COSET Must be Supplemented by “Model”  
for 4 or more-Point Interactions

(Constant Amplitude Not Good  
Model with Fermions)

Cascade Decay Tree of Sequential 2-Body Decays Well Defined States

COSET: Functional Form of the Leading Order Correlations are  
(Almost) Uniquely Determined by the Quantum Numbers and  
Masses

# COSET 2-Body Cascade Decay Correlations



To Leading Order in  $\Gamma/m$  - Single Invariant  $m_{23}^2$

$$(1 / \Gamma)(d \Gamma / dx) = f(x)$$

Odd Order Polynomial Degree  $4J+1$

$$x = m_{23} / m_{23}^{\max}$$

Have (Almost) Complete List

$J = 0, \frac{1}{2}$  Shape Independent of Masses

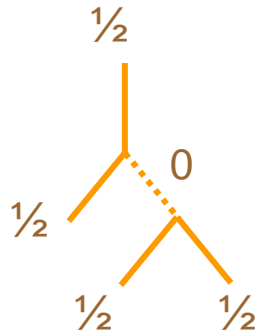
$J \geq 1$  Shape Depends on Masses

Gain Mass Through (Generalized) Higgs Mechanism :  
Coupling Through Longitudinal and Transverse  
Components Give Different Distributions

(Suggests Method for Determining Top Mass from  $m_{lb}$   
Independent of b-Jet Energy Scale Uncertainty)

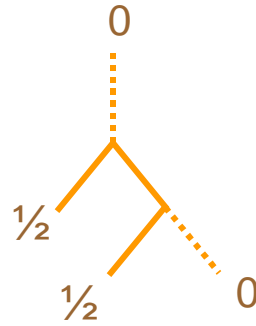
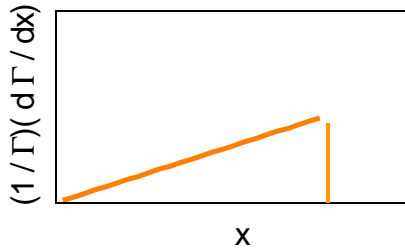


# COSET 2-Body Cascade Decay Correlations



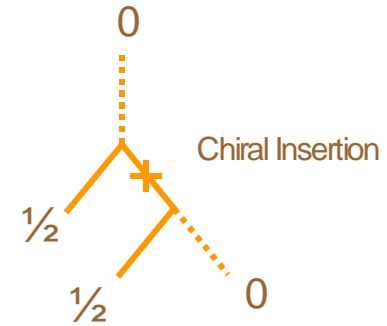
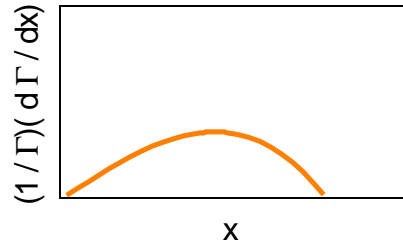
$$2x$$

Triangle



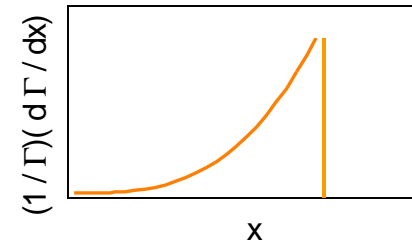
$$4x(1 - x^2)$$

Hump



$$4x^3$$

Half-Cusp



Unique Chiral Structure - Independent of Majorana/Weyl, Dirac, PseudoDirac, ...

See Michael's Talk on COSET Interpretation of Signatures Within SUSY

# Determining the Spin of Partner Particles

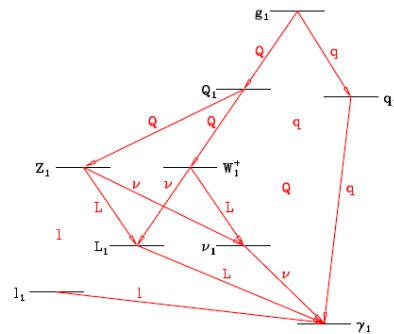
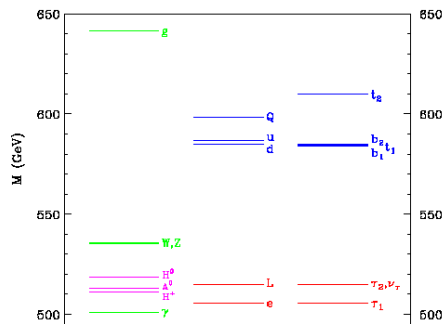
Assume Underlying Theoretical Framework:

Quadratic Divergences Cancelled by Partner Particles

Spin Differs by  $\Delta J = \frac{1}{2}$  SUSY

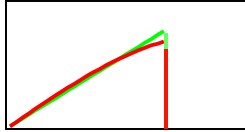
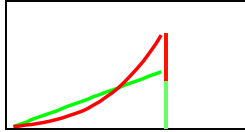
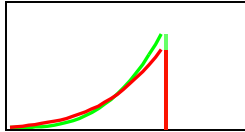
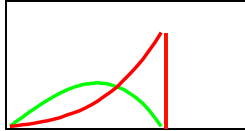
Same Spin  $\Delta J = 0$  One-Loop GIM

Example: Minimal Universal Extra Dimension



mSUGRA like Mass Ordering :  
 Adjacent Lepton-Lepton and Lepton-Jet in Decay Tree

# Determining the Spin of Partner Particles

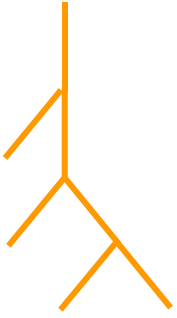
	Super-Partners	Same Spin-Partners (Nearly Degenerate)	SUSY Same Spin
Opposite-Sign Same-Flavor Lepton-Lepton	$2x$	$\frac{20}{9}x(1 - \frac{1}{5}x^2)$	
Jet-Lepton	$2x$	$\frac{2}{3}x(1 + 4x^2)$	
Opposite-Sign b-Jet-Lepton	$4x^3$	$\frac{2}{3}x(1 + 4x^2)$	
Same-Sign b-Jet-Lepton	$4x(1 - x^2)$	$\frac{2}{3}x(1 + 4x^2)$	

**Note:** No Initial state Charge Asymmetry Required

Better Discrimination with non-Degenerate States –  $O(x^5)$  Polynomial

Even Easier with Other Mass Orderings

# COSET Decay Trees



To Leading Order in  $\Gamma/m$  - Three Invariant  $m_{23}^2$   $m_{34}^2$   $m_{24}^2$

$$(1 / \Gamma)( d^3 \Gamma / dx dy dz ) = f(x,y,z)$$

$$x = m_{23}^2 / m_{23}^{\max}$$

$$y = m_{34}^2 / m_{34}^{\max}$$

$$z = m_{24}^2 / m_{24}^{\max}$$

In General  $f(x,y,z) \neq f(x)f(y)f(z)$  Although Possible

# (Reconstructed) Objects

Objects:

Leptons

Photons

Missing Transverse Energy

Jets

(Reconstructed) Object  $p^{\mu}$

Exotic Objects: New (Long Lived) States

Displaced Vertices - Leptons, Photons, Jets

Highly Ionizing Tracks

Highly Ionizing to Minimum Ionizing Kinks

Highly Ionizing Stopped Track

Out of Time Decays

Charge Exchange Tracks

Charge Changing Tracks

.....

High Multiplicity Mush

# To Exploit Correlations – Extract (Segment) of Decay Tree

In Addition to Standard Cuts ....

Invariant Correlations Can Also be Useful in Increasing Purity of Particular Decay Tree Within an Event Sample

Develop Discriminating Correlations Between Some Invariant Momenta or Correlation that Arises Within a Decay Tree and Some Other Variable(s)  
Apply Correlation to an Ensemble of Objects Within a Given Event

1. Reduces Combinatoric Confusion:

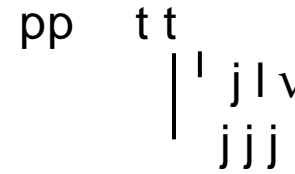
Incorrect Association – Invariants Unrestricted

2. Enhances Signal/Background Purity:

SM Background Tends to be at Worst Similar to Combinatoric Confusion of “Unrelated” Objects

Object Correlation Ensembles Extract Leading Order Trees (OCELOT)

# Semi-Leptonic Top Decay

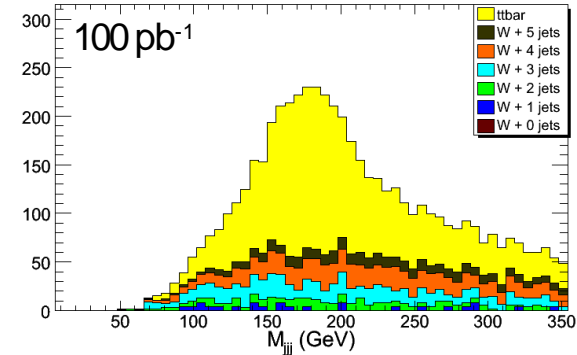


$N_{\text{jets}} \rightarrow 4$  with  $p_T > 30$  GeV

$N_{\text{muon}} \rightarrow 1$  with  $p_T > 20$  GeV

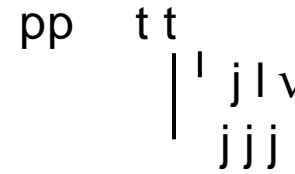
$H_T(\text{jets+muon+MET}) > 300$  GeV

CMSSW



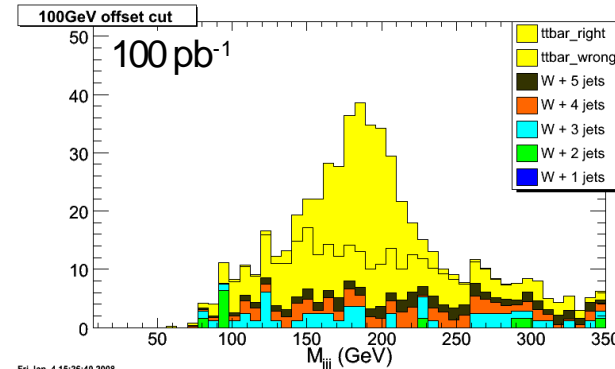
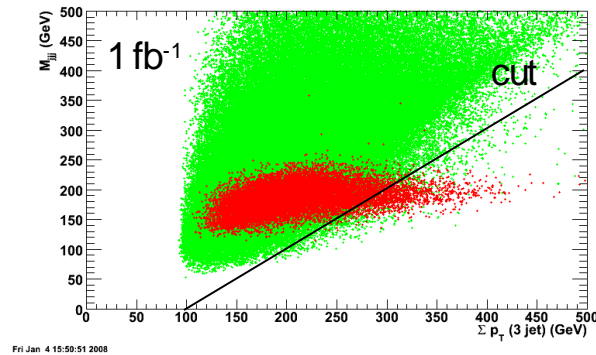
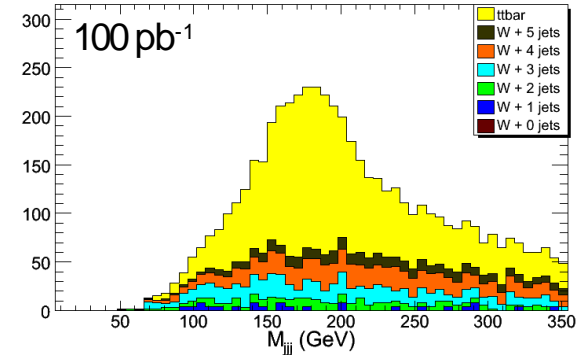
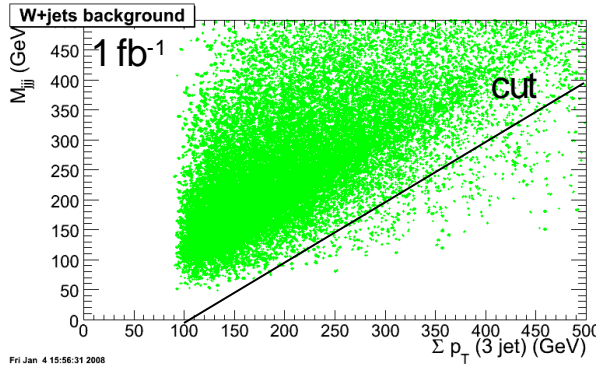
$m_{jjj}$  : Choose 3 jets with highest vector  $|\sum p_{T\text{jets}}|$

# Semi-Leptonic Top Decay - OCELOT



Correlation:  $f(m_{jjj}, \sum_{i=1,3} |p_{T,jeti}|)$   
 Ensemble All jets  $p_T > 30$  GeV

CMSSW



Note SM Background and Combinatoric Confusion (In Tails)

Purity Crucial in Reconstructing More Branches of Decay tree – SUSY,  $b'$ , .....

(Much) More Efficient Than Merged Top Jets



# Multi-jet Hadronic Resonances - OCELOT

Standard Techniques Inadequate Even for Extracting  
Hadronic Signal from QCD Background

See Eva's Talk on OCELOT for Purely Hadronic Multi-jet Resonances

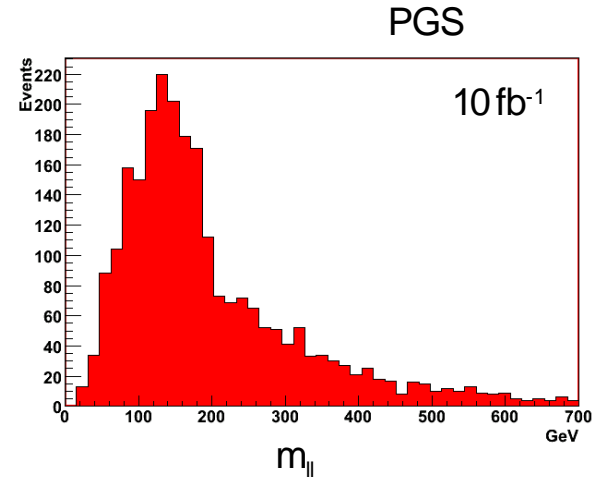
# Di-Lepton Correlations (Edges)

Standard SUSY Spectrum

$N_{\text{Jets}} > 2$  with  $p_{\text{T}} > 40$  GeV

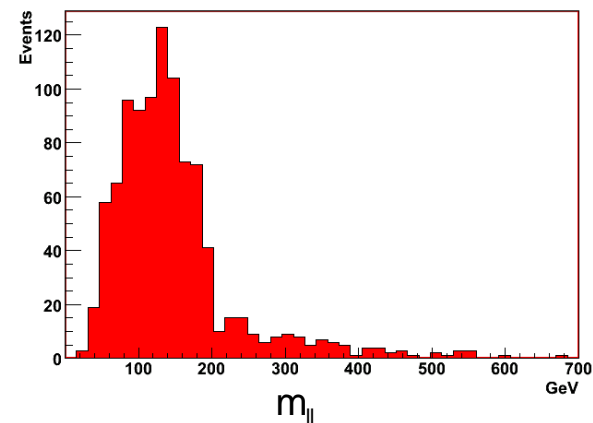
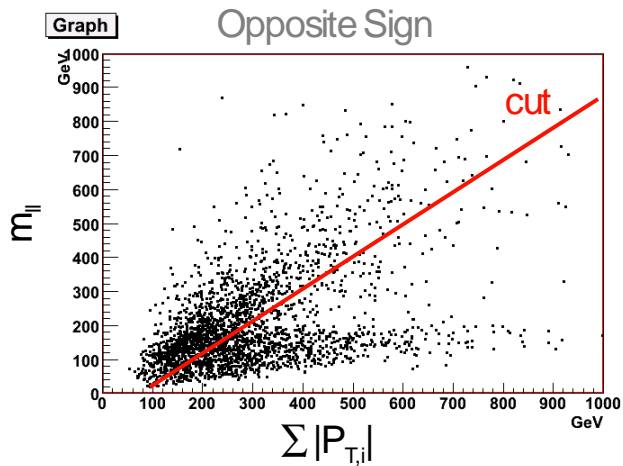
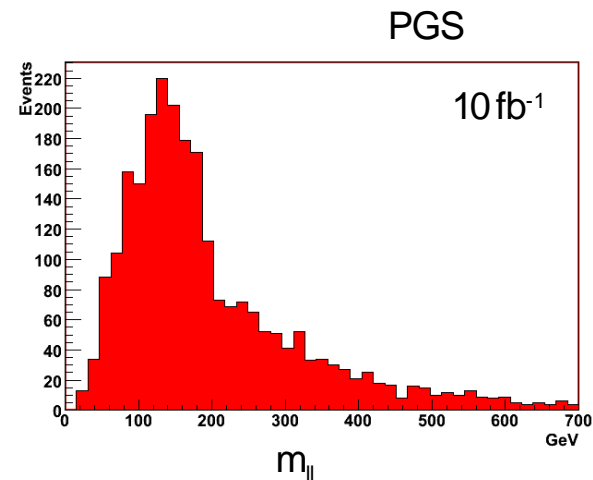
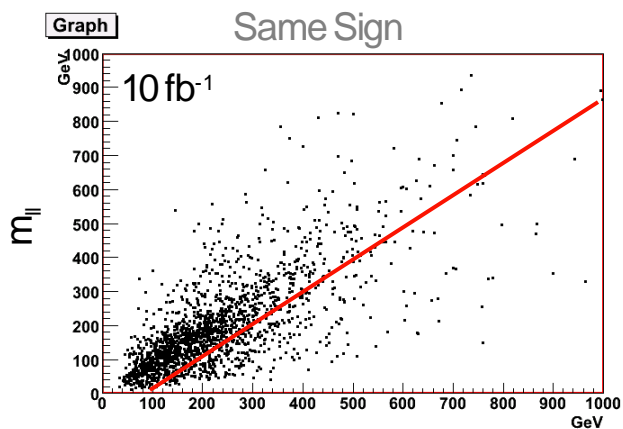
$N_{\text{Leptons}} > 3$  with  $p_{\text{T}} > 25$  GeV

$\text{MET} > 150$  GeV



# Di-Lepton Correlations (Edges) – OCELOT

Correlation:  $f(m_{ll}, \sum_{i=1,2} |p_{T,i}|)$

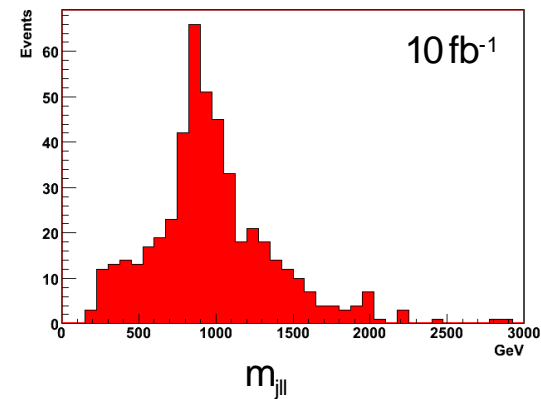
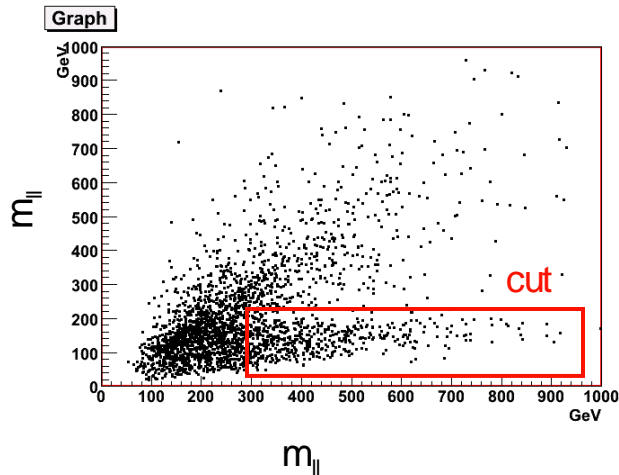
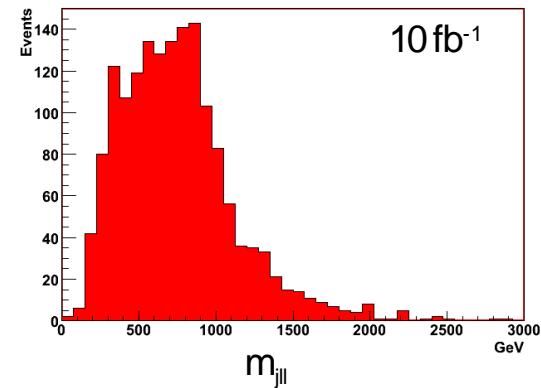
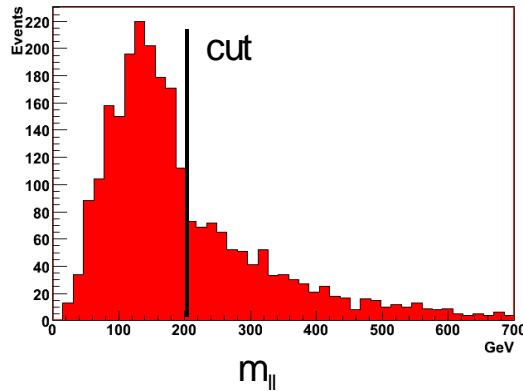


Horizontal Branch  
Diagonal Branch

Note: Tails - Edges at 150 and 190 GeV

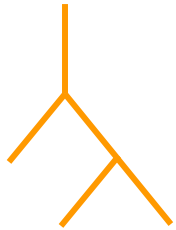
# Di-Lepton-Jet Correlations (Edges) – OCELOT

Invariant Momentum of Three Adjacent Branches  $jll$  in Decay Tree



Purity Important for Reconstructing Multi-Branched in Decay Tree

# Contained Decay Trees – OCELOT



To Leading Order in  $\Gamma/m$  - Single Invariant  $m_{23}$

Invariant Momentum of Two Branches  $m_{23}$  Completely Determines Correlations Within this Subprocess

Doesn't Hurt to Loose 3<sup>rd</sup> Branch to Missing Energy

(If Visible) Can Still use  $m_{12}$  and  $m_{13}$  to Form Additional Correlations

1. Extract More Information Directly from Correlations
2. Further Improve Signal to Background Contrast – Higher Dimensional Correlations

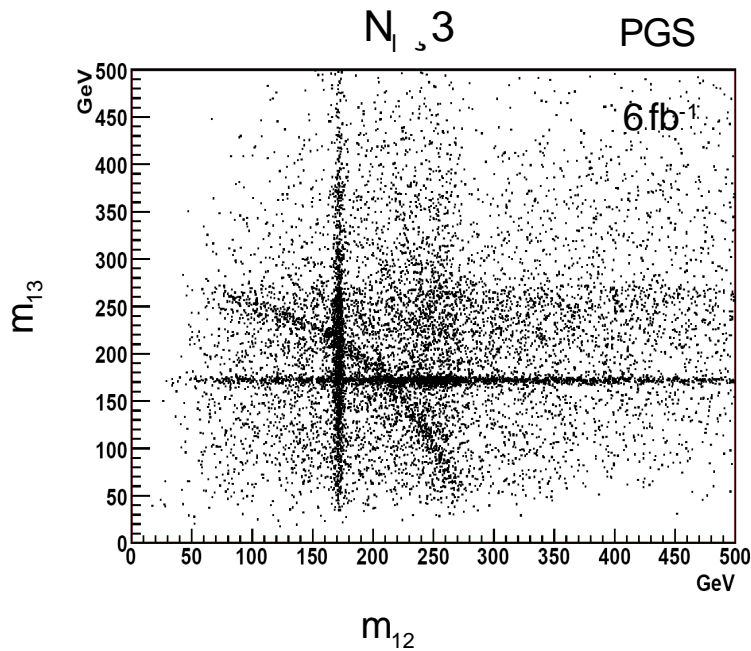
# Contained Decay Trees – OCELOT

- New Physics Sample

$$N_l = 2-6$$

$$N_{\text{jet}} \leq 2$$

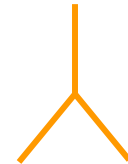
Backgrounds Unimportant



- Enhanced  $S/B_{\text{Combinatoric}}$  Contrast

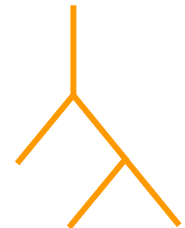
$$D_S < D_B \quad (D=1 \text{ Histogram } D_S = D_B)$$

- Two Body Resonant Tree

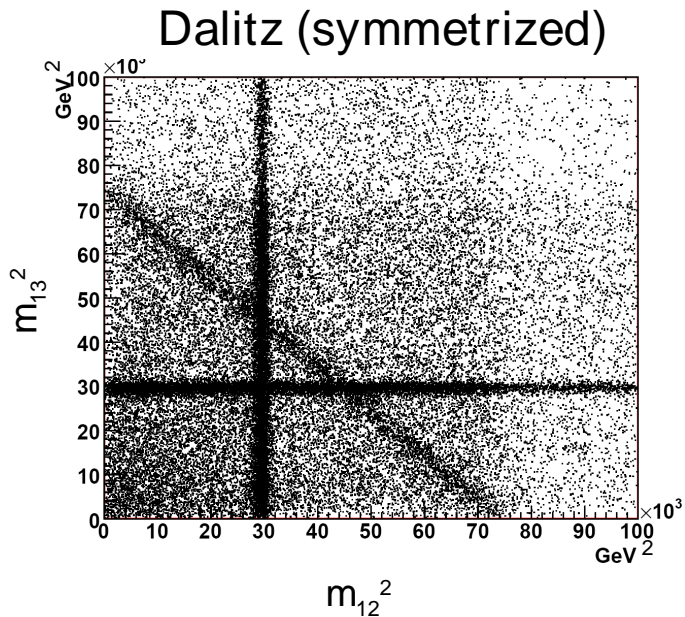


- Correlation  $m_{12}^2 + m_{13}^2 = \text{Constant}$

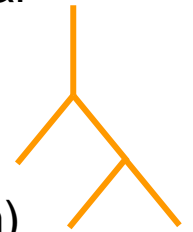
(Some of) The Two Body Resonances  
Arise from Three Body Decay



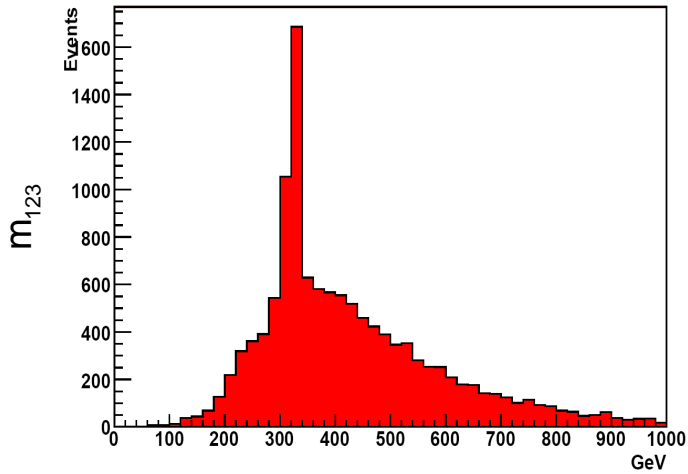
# Contained Decay Trees – OCELOT



- Uniform  $|M|^2$  on Two Body Resonances  
Consistent with Intermediate Scalar
- Edges
  - Three Body Tree (Only feature in D=1 Histogram)
  - Coincide with Endpoint of Resonant Two Body Correlation
    - Arise from “Missing” Lepton
    - Anything Else Contributing to Edge is massless
- Relative Density of Two Body Resonances, Resonant Two Body Correlation, and Edge Contrast
  - $\text{Br}(\Phi \text{ III}) / \text{Br}(\Phi \text{ IIX})$

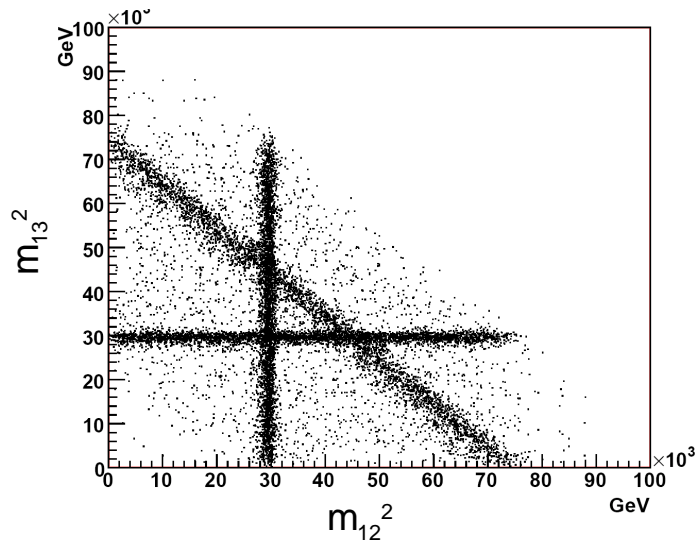
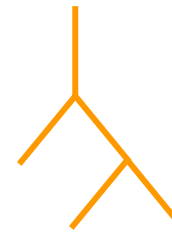


# Contained Decay Trees – OCELOT



Three Body Resonant Trees

310 GeV  $\cdot m_{III}$   $\cdot$  330 GeV



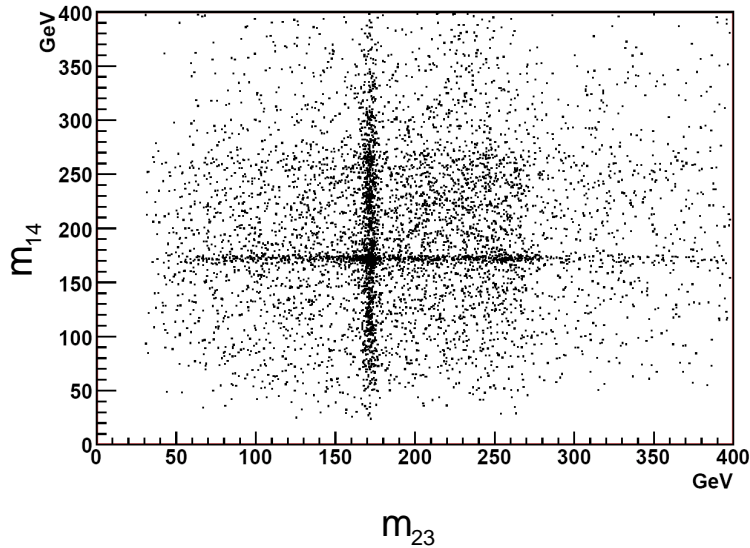
• Further Enhances

• S/B<sub>Combinatoric</sub> Contrast



# Inter-Tree Correlations – OCELOT

$N_{\text{, } 4}$



- No Kinematic Correlation (factorize)
  - Consistent with Arising from Different Parent Particle
- $m_{14} = m$  and  $m_{23} \neq m$  or  $m_{14} \neq m$  and  $m_{23} = m$ 
  - Single Resonant Two Body Decay

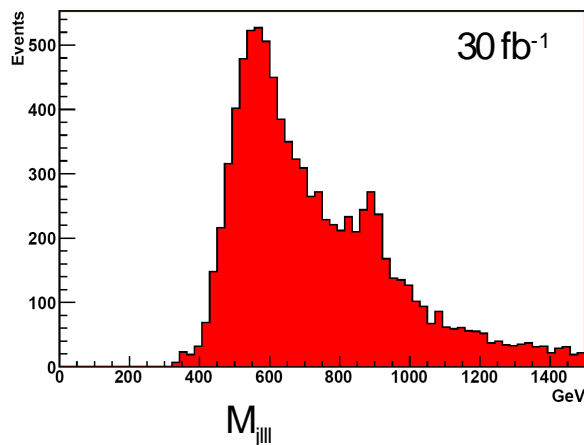
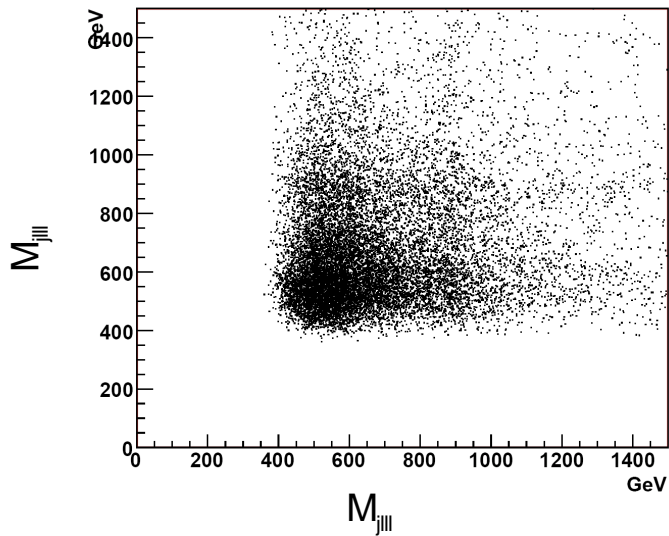


- $m_{14} = m_{23} = m$ 
  - If Density at Intersection  $\text{, } 2$  Some Events with (At least) Two Resonant Two Body Decays
  - Density at Intersection gives Fraction

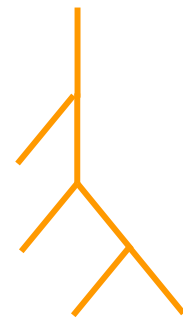


# Contained Di-Lepton-Jet Correlations – OCELOT

$N_{j, \geq 2}$



- Contrast  $S/B_{\text{Combinatoric}}$  Contrast Improved
- Two Four Body Resonant Decays



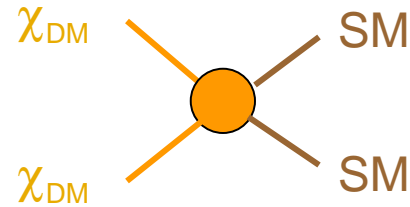
- Density in Bands and Intersections Give

$$\sigma \text{ Br}(\Psi_1 \rightarrow jll) / \sigma \text{ Br}(\Psi_2 \rightarrow jll)$$

- Correlation Could Indicate Resonant  
• Five Body Decay  $\xi \rightarrow jjll$

# Determining the Stabilizing Symmetry of WIMP Dark Matter

WIMP Dark Matter – Freeze Out  
 Requires Stabilizing (Exact) Symmetry

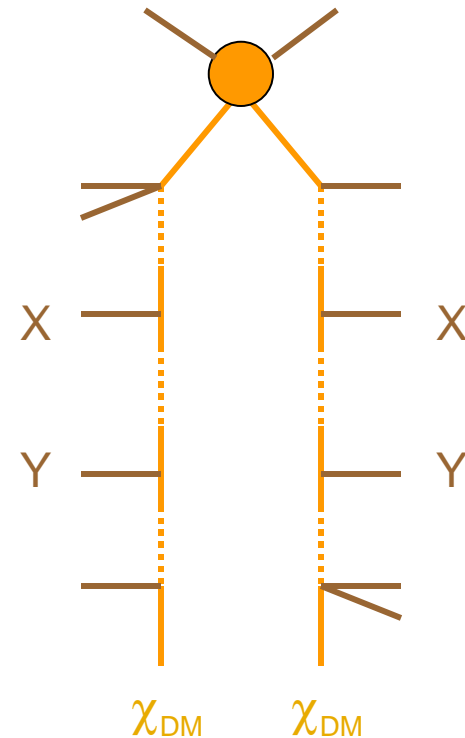


$m \chi \chi$  Allowed - SM Uncharged

Abelian

Continuous	U(1)	$(X+Y)(X-Y)$	Opposite Sign
Discrete	$Z_2$	$(X+Y)(X-Y)$	Opposite Sign
		$(X+Y)(X+Y)$	Same Sign

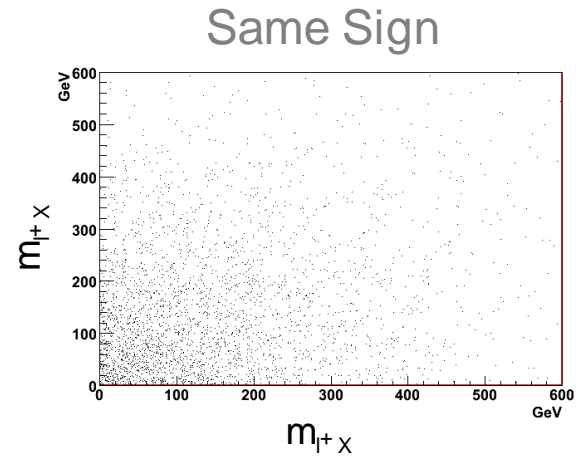
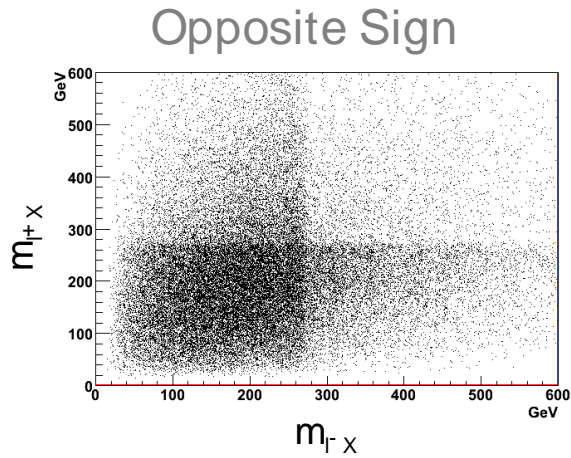
(Small Caveats)



# Inter-Tree Correlations - OCELOT

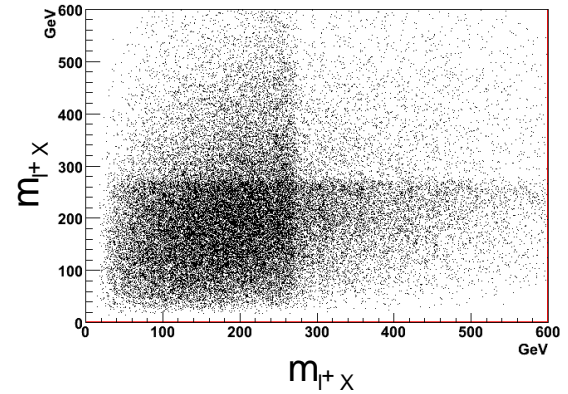
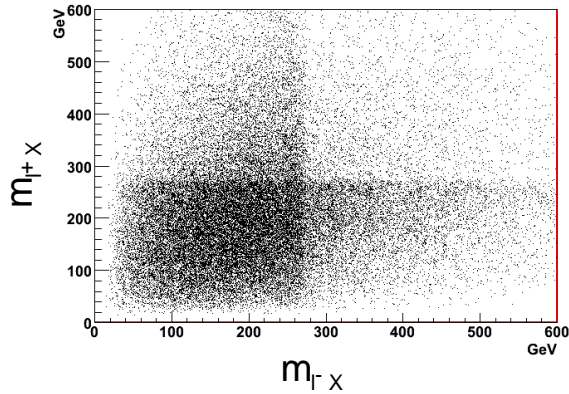
Simultaneous COSET  $m_{XY} - m_{XY}$  Inter-Tree Correlation (factorizes)

Continuous



25 fb<sup>-1</sup>

Discrete



Note: Same-Sign vs Opposite Sign - Count **NOT** Sufficient

# Object Correlations

- Correlations in Generalized Dalitz Space  $m_{ij}^2$  Provide Direct Path to Masses, Quantum Numbers, Spins, and Interactions of New States  
Direct Solution to the Inverse Problem
- Consistent OnShell Effective Theory (COSET) for Decay Tree Correlations . (Almost) Uniquely Determines Leading Order Correlations for Sequential . 2-body Decays  
Spin  $J = 0 + \frac{1}{2}$  Only Three Correlations for Adjacent Branches  
.Higher Spins Correlations Depend on Masses  
Spin Determination Can be Relatively Easy
- Object Correlation Ensembles for Leading Order Trees (OCFLOT) Improve Purity of Particular Decay (Sub)Tree within an Event Sample  
Higher Dimensional Correlations can Further Improve ....
- Correlations Can Play a Direct Role in Determining Underlying Theoretical Framework











Rather Direct Path from Data to Interpretation – Early Inverse Problem

Reduce Combinatoric Confusion

Ensemble Technique Very Useful – and Should Have Wide Applicability

Here boosted ... Compare Hemisphere --

Correlations in Generalized Dalitz space

Kinematic Correlations Can Enhance Contrast  $DS < DB$

Develop Templates (Neural Nets) for  
Generalization to Higher Dimensional Correlations of Edges and Endpoints

Correlations Allow Direct Measurements

Implement Correlations in Fitting

Procedure to Decay Trees

. (Fitting to  $D=1$  Counts Misses Many Correlations)

## Order for COSET

0. n-body ..... (note constant  $|M|^2$  not good ....)
3. List of COSET amplitudes
4. General polynomial of spin ....
5. Focus on Adjoint branches spin=0,1/2 – three shapes
6. Pick something(s) – what you learn – completely Mind
7. Determining Partner particle spins (UED as example)
8. Top quark Couplings ..... (don't mention – not “new” Physics)
9. SUSY Michael .....
10. Reconstructing Decay Chains .....

	Super-Partners	Same Spin-Partners (Nearly Degenerate)
Opposite-Sign Same-Flavor Lepton-Lepton	$2x$	$\frac{20}{9}x(1 - \frac{1}{5}x^2)$
Jet-Lepton	$2x$	$\frac{2}{3}x(1 + 4x^2)$
Opposite-Sign b-Jet-Lepton	$4x^3$	$\frac{2}{3}x(1 + 4x^2)$
Same-Sign b-Jet-Lepton	$4x(1 - x^2)$	$\frac{2}{3}x(1 + 4x^2)$

$$f(p_i^2) = f_0 + (p_i^2 - m_i^2) \frac{\partial f(p_i^2)}{\partial (p_i^2 - m_i^2)} + \dots \quad i = 1, 2, 3$$

$$\langle \Psi_0(p) \Psi_0(-p) \rangle = -2\pi i \delta(p^2 - m^2) + \dots$$

$$\langle \psi(p) \psi(-p) \rangle = P \left( \frac{1}{p^2 - m^2} \right)$$

$$\psi_i \psi_j \phi + \text{h.c.}$$

$$\psi_i^* \sigma^\mu \psi_j A_\mu$$

$$\psi_i \sigma^{\mu\nu} \psi_j F_{\mu\nu} + \text{h.c.}$$

$$\phi_{(i} \partial^\mu \phi_{j)} A_\mu$$

$$\phi_{[i} \partial^\mu \phi_{j]} A_\mu$$

$$f(p_i^2) = f_0 + (p_i^2 - m_i^2) \frac{\partial f(p_i^2)}{\partial (p_i^2 - m_i^2)} + \dots \quad i = 1, 2, 3$$

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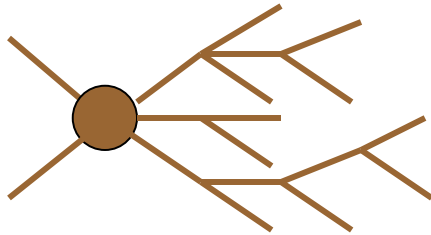
$$\phi_{(i} \partial^\mu \phi_{j)} A_\mu$$

$$\phi_{[i} \partial^\mu \phi_{j]} A_\mu$$

# New Physics at the Large Hadron Collider

- Extract Signatures from Data
- Interpret Signatures
- Determine Underlying Theoretical Framework

Put what can measure here – then RECO next – with kinematics on same page



Hard Scattering Processes -  
Produce Low Multiplicity States -  
Decay to “Stable” SM Particles

## (Reconstructed) Objects

Leptons  
Photons  
Missing Transverse Energy  
Jets

(Reconstructed) Object  $p^\mu$

Exotic Objects (New Long Lived Particles)

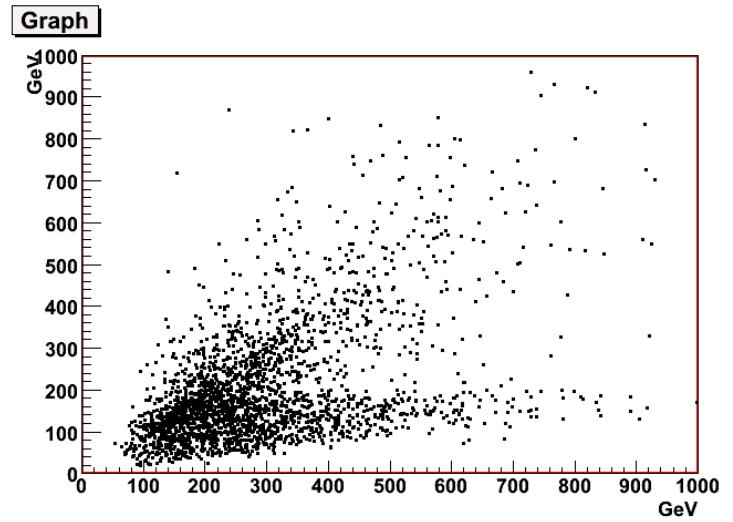
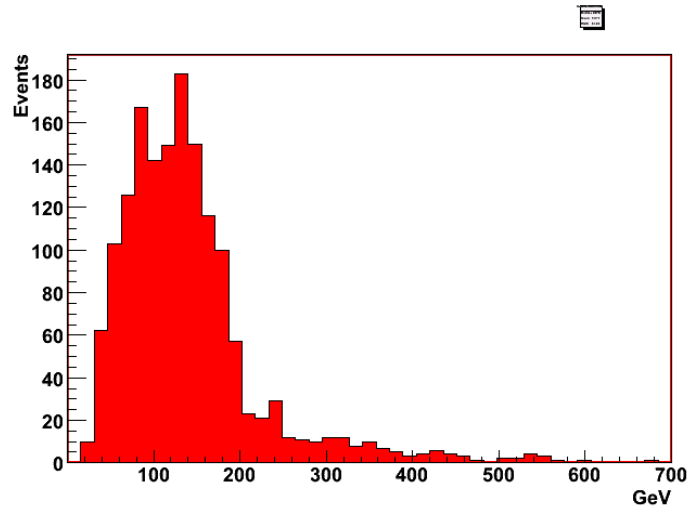
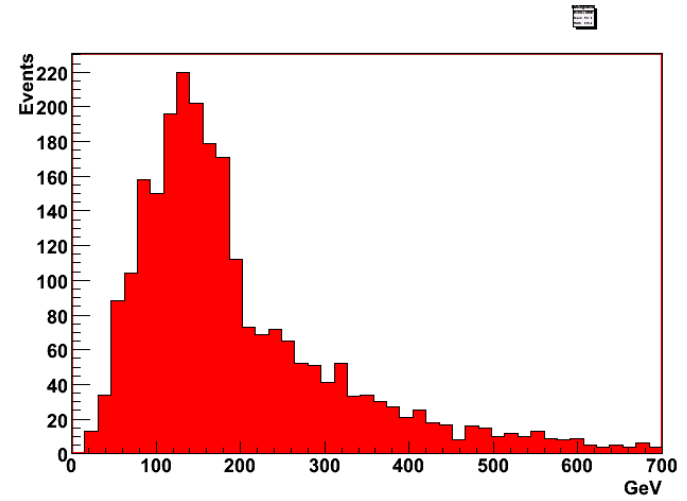
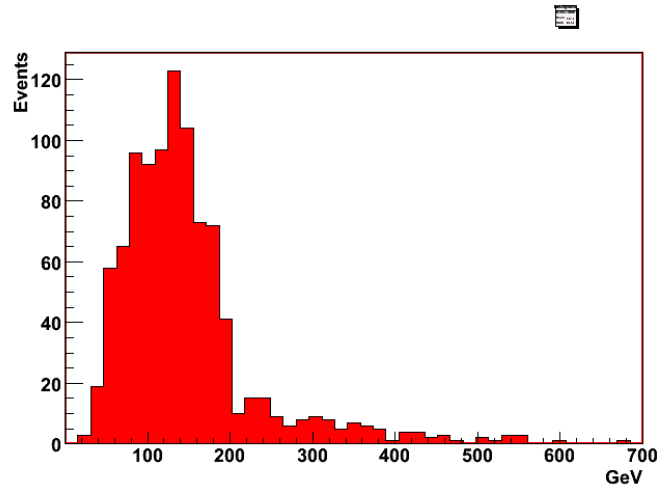
Displaced Vertices - Leptons, Photons, Jets  
Highly Ionizing Tracks

Highly Ionizing to Minimum Ionizing Kinks  
Highly Ionizing Stopped Track

Out of Time Decays

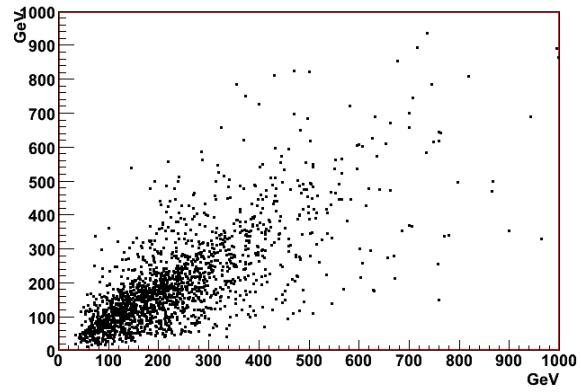
Charge Exchange Tracks  
Charge Changing Tracks

.....

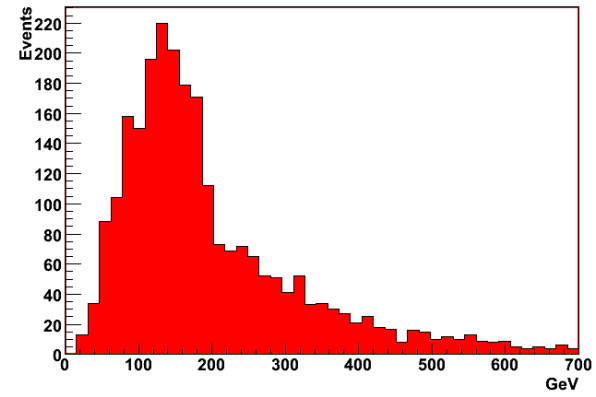




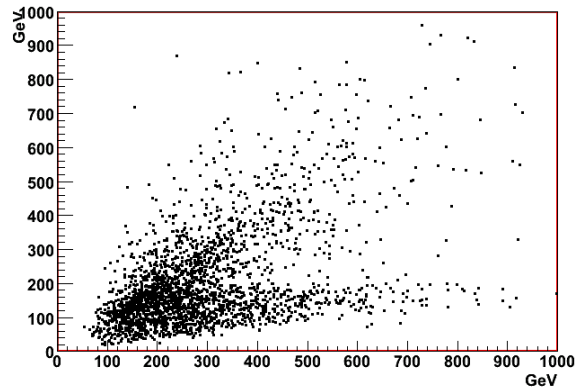
Graph



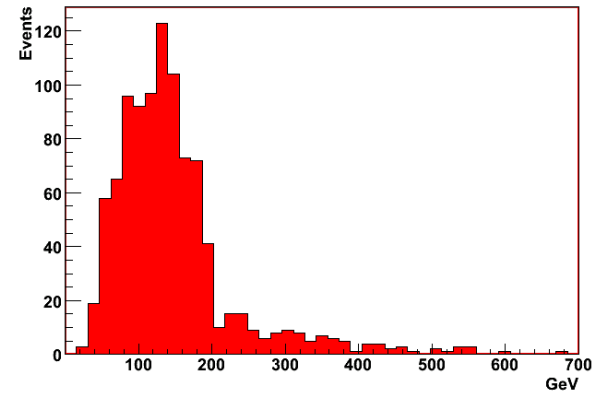
Graph



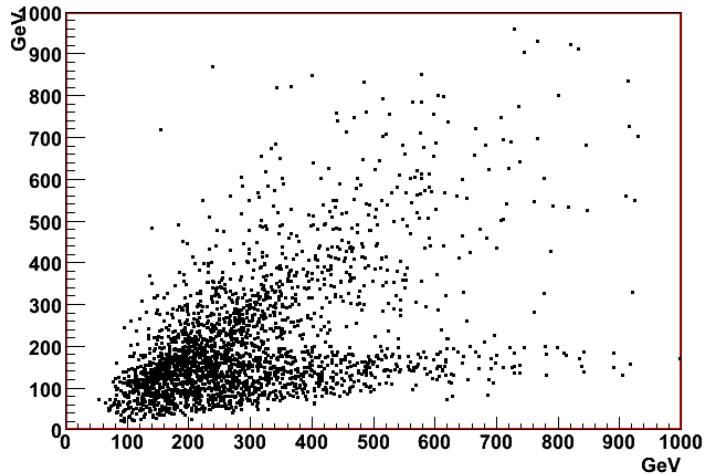
Graph



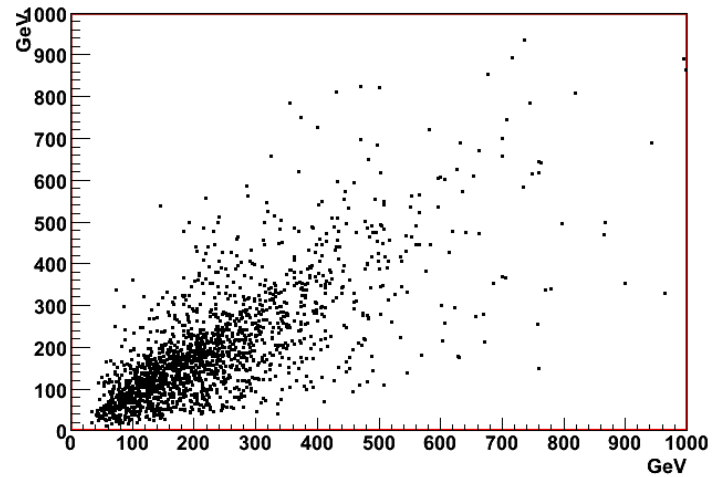
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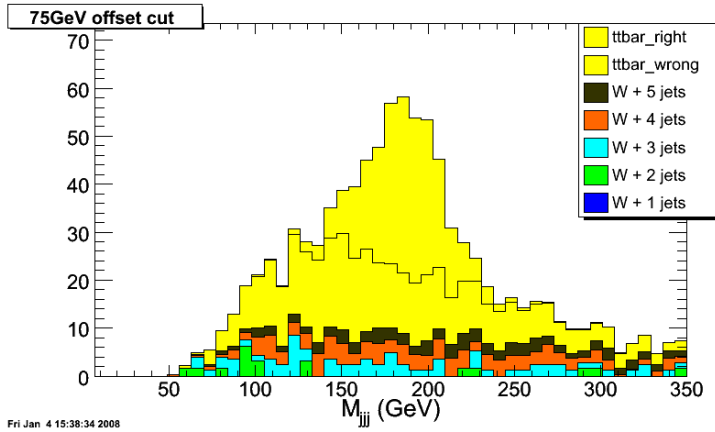


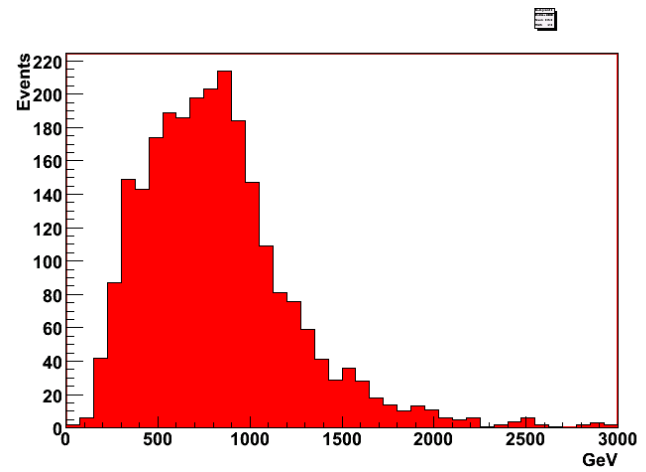
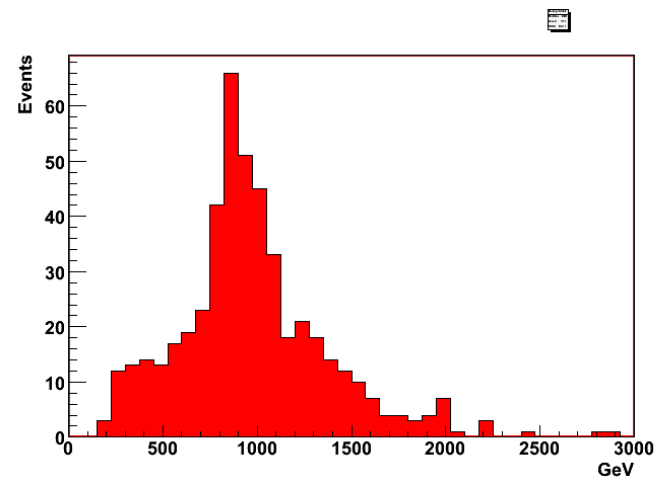
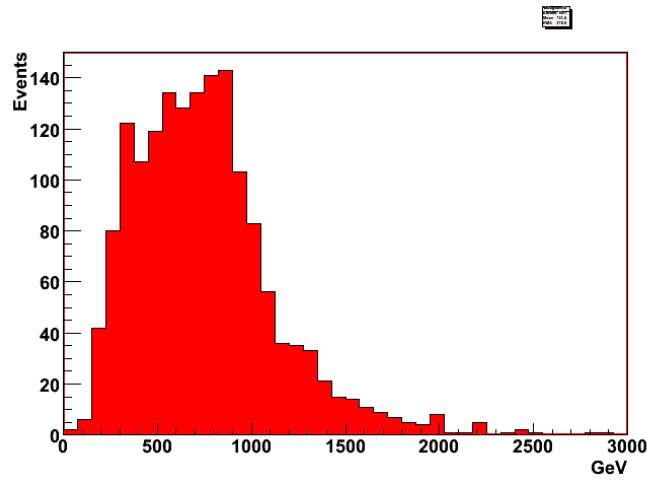
Graph



Graph

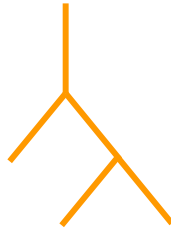






# Kinematic Correlations

Decay Trees



Invariant Kinematic Correlations =  $f(m_{ijk\dots}^2)$

(Unpolarized,  
Spins Unobserved,  
T-Invariance)

$$m_{ijk\dots}^2 = f(m_{ij}^2)$$

Correlations in Generalized Dalitz Space  $m_{ij}^2$   $i,j$  = All Pairs of Objects

Correlations Isolate ... Background and Combinatoric Confusion

Can make use of correlations Also to reduce background

Use Other Variable sPull Apart Correct pairing of signal Always Correct

Don't forget to TITLE OCELO

Order for OCELOT Correlations

RECO FIRST I guess

2. semi-leptonic top Dmitry
3. Jets – Eva ..... (understand efficiency)
4. Lepton edge
5. Llj distribution
6. Resonant stuff If visible redundant – If all visible although redundant can still use to form additional correlations and extract more information but still can make use of it ..... Resonant
8. Dark Matter

# Object Correlations to Extract Low Order Trees (OCELOT)

Kinematic Correlations Can Enhance Contrast  $D_S < D_B$

Menu of Correlations for Low Order Trees

- Develop Templates to Search for Correlations

Extend to Trees with MET

(Generalization to  $D > 1$  of Edges and Endpoints)

Correlations Allow Direct Measurements

Implement Correlations in Fitting Procedure to Decay Trees

- . (Fitting to  $D=1$  Counts Misses Many Correlations)